STAT/MA 41600

In-Class Problem Set #39: November 24, 2014

- 1. Roll two 6-sided dice. Let X denote the minimum value, and let Y denote the maximum value.
- **1a.** Find the covariance of X and Y.
- **1b.** Find the correlation of X and Y.
- 2. Suppose that 6 students come to a party, and each of them brings their favorite CD with them. (For convenience, assume that they each have a different favorite CD.) As they leave the party, they take a CD at random as they depart. Let X denote the number of students who get their own CD back. Find Var(X).
- **3.** Draw 5 cards from a 52 card deck (without replacement).
- **3a.** Let X denote the number of Hearts that appear. Find $\mathbb{E}(X)$ and also Var(X).
- **3b.** Let Y denote the number of Queens that appear. Find $\mathbb{E}(Y)$ and also $\mathrm{Var}(Y)$.
- **3c.** Find the covariance of X and Y.
- **4.** Consider a pair of random variables X, Y with constant joint density on the quadrilateral with vertices located at the points (0,0), (3,0), (5,2), (0,2).
- **4a.** Find the covariance of X and Y.
- **4b.** Find the correlation of X and Y.
- **5.** Suppose that X and Y have a constant joint density on the triangle with vertices (0,0),(3,0),(0,3).
- **5a.** Find the covariance of X and Y.
- **5b.** Find the correlation of X and Y.
- **6.** Suppose X and Y have joint probability density function

$$f_{X,Y}(x,y) = 60e^{-4x-6y}$$

for 0 < x < y; and $f_{X,Y}(x,y) = 0$ otherwise. We already saw, on Midterm Exam #2, that $\mathbb{E}(X) = 1/10$.

- **6a.** Find $\mathbb{E}(Y)$.
- **6b.** Find $\mathbb{E}(XY)$.
- **6c.** Use what you know to find the covariance of X and Y.