

Counting: Recall if sample space S has equally likely outcomes, and S has finite size, then an event A has probability

$$P(A) = \frac{|A|}{|S|} = \frac{\# \text{ of outcomes in } A}{\# \text{ of outcomes in } S}.$$

Roll 2 dice

	1	2	3	4	5	6
1	✓					
2	✓	✓				
3	✓	✓	✓			
4	✓	✓	✓	✓		
5	✓	✓	✓	✓	✓	
6	✓	✓	✓	✓	✓	✓

Let X denote the result on the red die
 Let Y denote the result on the green die.

$$P(X \geq Y) = \frac{|A|}{|S|} = \frac{21}{36} = \frac{7}{12}$$

"A" denote the event that $X \geq Y$
 i.e. that the outcome ω makes $X(\omega) \geq Y(\omega)$

Another example: Let $Z = \min(X, Y)$. Find $P(Z \leq 3)$.

	1	2	3	4	5	6
1	✓	✓	✓	✓	✓	✓
2	✓	✓	✓	✓	✓	✓
3	✓	✓	✓	✓	✓	✓
4	✓	✓	✓	✓	✓	✓
5	✓	✓	✓	✓	✓	✓
6	✓	✓	✓	✓	✓	✓

min = 1 (11 outcomes)
 min = 2 (9 outcomes)
 min = 3 (7 outcomes)

$$P(Z \leq 3) = \frac{27}{36} = \frac{3}{4}$$