

Expected value and variance of a Beta random variable

$$\text{In general: } E(X) = \frac{\alpha}{\alpha + \beta} \quad \text{Var}(X) = \frac{\alpha\beta}{(\alpha + \beta)^2(\alpha + \beta + 1)}$$

Do not need to derive these in the general case.

We focus on specific α and β values, and when we fix specific α and β then we can derive the expected value and variance.

$$\text{Notice: } f_X(x) = \begin{cases} \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1} & \text{for } x \in [0, 1] \\ 0 & \text{otherwise} \end{cases}$$

This Γ function is just a factorial of the input minus 1, when the input is an integer. i.e. $\Gamma(n) = (n-1)!$ for integers n .

$$\Gamma(5) = 4!, \quad \Gamma(8) = 7!, \text{ etc.}$$