

If X is a Normal random variable with parameters μ_x, σ_x^2 , then claim $\frac{X - \mu_x}{\sigma_x}$ is a standard normal random variable.

First, $\frac{X - \mu_x}{\sigma_x} = \left(\frac{1}{\sigma_x}\right)X - \left(\frac{\mu_x}{\sigma_x}\right)$ then it is a normal random variable.

$$\text{Also } E\left(\frac{X - \mu_x}{\sigma_x}\right) = \frac{E(X - \mu_x)}{\sigma_x} = \frac{E(X) - \mu_x}{\sigma_x} = 0$$

$$\text{Var}\left(\frac{X - \mu_x}{\sigma_x}\right) = \frac{1}{\sigma_x^2} \text{Var}(X - \mu_x) = \frac{1}{\sigma_x^2} \text{Var}(X) = 1$$

So $\frac{X - \mu_x}{\sigma_x}$ must not just be any normal random variable, but moreover a standard normal random variable.

We must always remember to convert Normal random variables to standard normal random variables when using the CDF chart.

E.g. Say X is a normal random variable with $\mu_x = 9$, $\sigma_x^2 = 5^2 = 25$
i.e. $\sigma_x = 5$

$$\text{Find } P(X \leq 12) = P\left(\frac{X - 9}{5} \leq \frac{12 - 9}{5}\right)$$

$$= P\left(Z \leq \frac{3}{5}\right) = P(Z \leq .6) = \boxed{.7257}$$

$$= F_Z(.6)$$

from the CDF table
for standard normal
random variables