

Example: Say X_1, X_2, \dots, X_{100} are independent Normal random variables, each with mean 3 and variance 5.

Find the probability that the sum of the X_j 's does not exceed 313.

$$P(X_1 + X_2 + \dots + X_{100} \leq 313)$$

$$= P\left(\frac{X_1 + X_2 + \dots + X_{100} - (100)(3)}{\sqrt{100(5)}} \leq \frac{313 - (100)(3)}{\sqrt{100(5)}}\right)$$

$$= P(Z \leq 0.58)$$

$$= F_Z(0.58)$$

$$= 0.7190$$

where Z is a standard normal random variable