

Approximating a Binomial random variable by a Standard Normal random variable - we must scale and shift the Binomial random variable appropriately.  $Z \approx \frac{X - np}{\sqrt{npq}}$

Similarly we can use a Normal approximation to Poisson random variables with large parameter  $\lambda$ .

In other words, if  $X$  is a Poisson random variable with large parameter  $\lambda$ , then  $\frac{X - \lambda}{\sqrt{\lambda}}$  is approximately distributed

like a standard normal random variable.

(To think about why this is true, write the Poisson  $X$  as a sum of  $\lambda$  Poisson random variables that are each having parameter 1 and that are independent, if  $\lambda$  is an integer.)

E.g. Suppose  $X$  is a Poisson random variable with  $\lambda = 700$ .

Approximate  $P(X \leq 730) = P(X \leq 730.5)$

$$\begin{array}{cccccc} | & | & | & | & | & | \\ \hline 728 & 729 & 730 & 731 & 732 & \\ \checkmark & \checkmark & \checkmark & \text{NO} & \text{NO} & \end{array} \quad = P\left(\frac{X - 700}{\sqrt{700}} \leq \frac{730.5 - 700}{\sqrt{700}}\right) \\ \approx P(Z \leq 1.15) = 0.8749$$

By the way, the exact value is

$$P(X \leq 730) = \sum_{j=0}^{730} \frac{e^{-700} 700^j}{j!} = 0.8750977\dots$$

The approximation is pretty good!