

One note: If X and Y are independent, then $E(X|Y=y) = E(X)$.

Why? If X is discrete:

$$E(X|Y=y) = \sum_x (x) \underbrace{p_{X|Y}(x|y)}_{= p_X(x) \text{ if } X, Y \text{ indep.}} = \sum_x (x) p_X(x) = E(X).$$

If X is continuous:

$$E(X|Y=y) = \int_{-\infty}^{\infty} (x) \underbrace{f_{X|Y}(x|y)}_{= f_X(x) \text{ if } X, Y \text{ indep.}} dx = \int_{-\infty}^{\infty} (x) f_X(x) dx = E(X).$$