1. **Winnings and Losing.** (a.) Since $X$ is Geometric with probability of success 0.40, he expects to play $E(X) = 1/0.40 = 2.5$ games.

(b.) Since $X$ is Geometric with probability of success 0.40, the variance of the number of games he plays is $\text{Var}(X) = 0.60/(0.40^2) = 3.75$.

(c.) The probability that he plays 4 or more games is equal to the probability that the first three games are all losses, i.e., $(0.6)^3 = 0.216$.

2. **Winnings and Losing (continued).** (a.) His gain or loss is $Y = 5 + (-4)(X - 1) = 9 - 4X$, since he wins 1 game and loses $X - 1$ games.

(b.) His expected gain/loss is $E(Y) = E(9 - 4X) = 9 - 4E(X) = 9 - 4(2.5) = -1$.

(c.) The variance of his gain/loss is $\text{Var}(Y) = \text{Var}(9 - 4X) = 16 \text{Var}(X) = 16(3.75) = 60$.

3. **Telemarketers.** Here $X$ is Geometric with probability of success $1/8$, because “success” denotes a call from the telemarketer. So $X > n$ if the first $n$ calls are unsuccessful, i.e., if the first $n$ calls are not telemarketers. So $P(X > n) = (7/8)^n$.

4. **Dating.** (a.) Since $X$ is Geometric with probability of success $.07$, then $E(X) = 1/.07 = 100/7 = 14.29$.

(b.) Since $X$ is Geometric with probability of success $.07$, then $\text{Var}(X) = .93/(.07)^2 = 189.8$.

(c.) Since $X$ is memoryless, then given $X > 3$, the remaining $Y = X - 3$ people we need to call is also Geometric with probability of success $.07$. So the mass of $Y$ given $X > 3$ is $P(Y = y | X > 3) = (.93)^{y-1}(.07)$ for integers $y \geq 1$, and $p_Y(y) = 0$ otherwise.

5. **Hearts.** (a.) Since $X$ is Geometric with probability of success $1/4$, then you expect to draw $E(X) = 1/(1/4) = 4$ cards to see the first heart.

(b.) Since $X$ is memoryless, then since we are given that the first 5 cards are not hearts, it follows that the additional number of cards (after the first five are drawn) is also Geometric, with probability of success $1/4$. So we expect to draw an additional $1/(1/4) = 4$ cards to see the first heart (after those first five are already drawn). (I.e., we expect that the first heart appears after 9 cards altogether.)