

STAT/MA 41600  
In-Class Problem Set #31: October 26, 2016

**1.** Consider two independent random variables  $X$  and  $Y$  that are each uniformly distributed on the interval  $[0, 10]$ .

Find  $P(|X - Y| < 1)$ , i.e., find the probability that  $X$  and  $Y$  are less than 1 unit apart. Hint: Think about the  $10 \times 10$  grid where  $(X, Y)$  is located. What is the area of the region where  $|X - Y| < 1$ ?

**2.** Suppose that the grades of two students are independent and each are uniformly distributed in the interval  $[90, 100]$ . Find the probability that the sum of the two grades is 197 or higher.

**3.** Suppose that  $U$  is uniformly distributed on the interval  $[0, 5]$ .

**3a.** What is the CDF of  $U$ ?

**3b.** Now define  $X = 3U + 2$ . What is the CDF of  $X$ ?

**3c.** What kind of distribution does  $X$  have?

**4.** Let  $U$  and  $V$  be independent and uniformly distributed on the interval  $[0, 3]$ .

Let  $X = \max(U, V)$ . Let  $Y = \min(U, V)$ .

**4a.** What is the CDF of  $X$ ?

**4b.** What is the probability density function of  $X$ ?

**4c.** What is the CDF of  $Y$ ?

**4d.** What is the probability density function of  $Y$ ?